

SCS 139

II.4 Alternating Current

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$$v_R = i_R R$$

$$i_C = C \frac{dv_C}{dt}$$

$$v_L = L \frac{di_L}{dt}$$



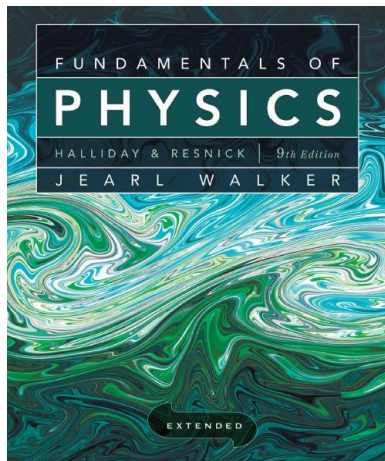
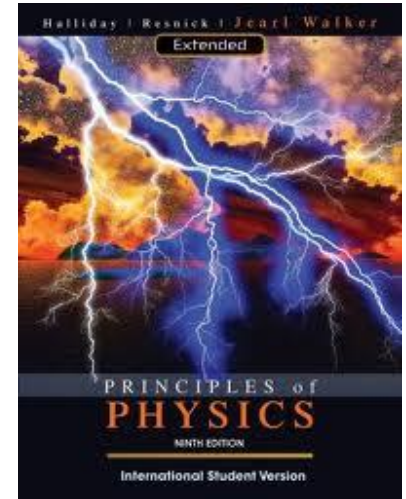
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Reference

- Principles of Physics
- Ninth Edition, International Student Version
- David Halliday, Robert Resnick,
and Jearl Walker

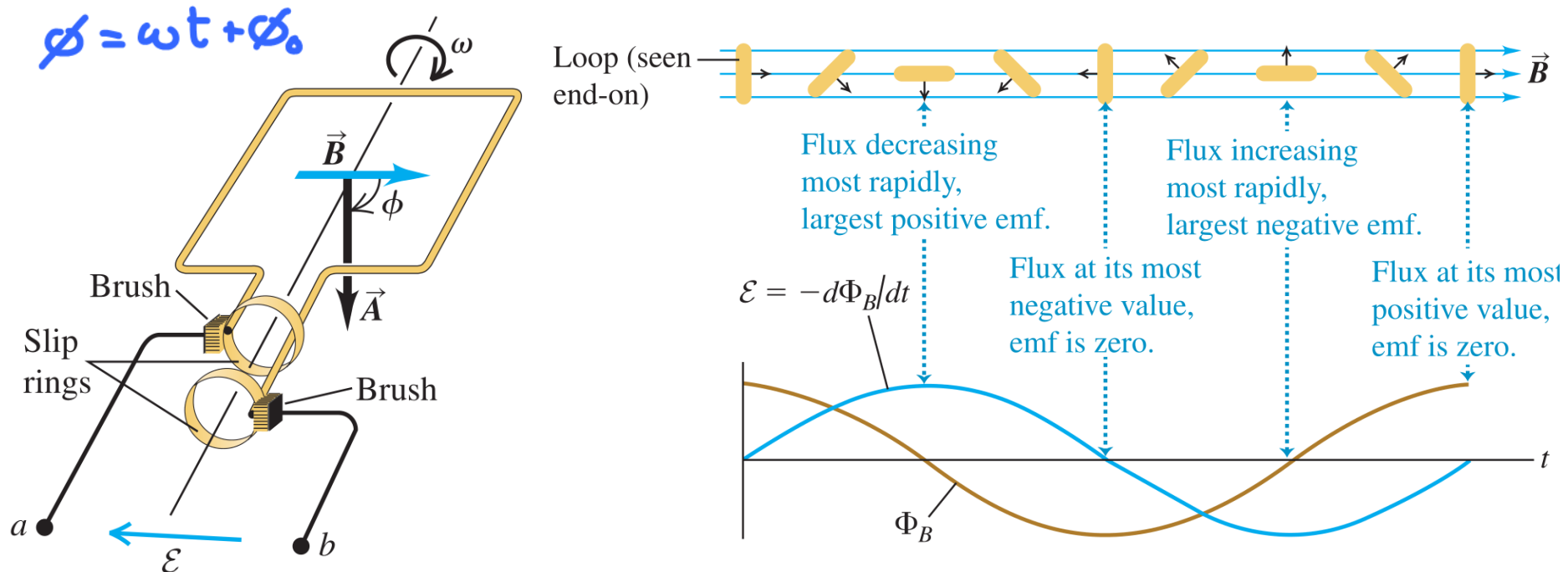


- Chapter 31
 - 31-6 Alternating Current
 - 31-7 Forced Oscillations
 - 31-8 Three Simple Circuits

$$\Phi_B = BA \cos \theta \Rightarrow \mathcal{E}_{ind} = -N \frac{d\Phi_B}{dt} = -BA(-\sin \theta) \frac{d\theta}{dt}$$

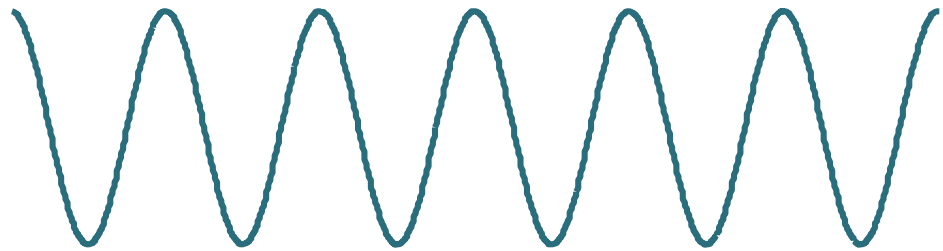
Alternating-Current Generator

- A conducting loop rotates (with constant angular speed ω) in an external (uniform and constant) magnetic field.

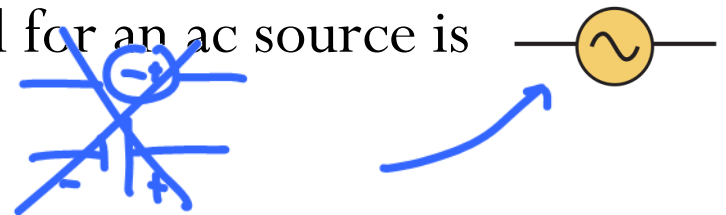


- Connections from each end of the loop to the external circuit are made by means of that end's slip ring.

Sinusoids



- A **sinusoid** (or sinusoidal signal) is a signal (e.g. voltage or current) that has the form of the sine or cosine function.
 - Turn out that you can express them all under the same notation using only cosine (or only sine) function.
 - **We will use cosine.**
- A sinusoidal current is referred to as **alternating current** (ac).
- Circuits driven by sinusoidal (current or voltage) sources are called **ac circuits**.
 - We use the term **ac source** for any device that supplies a sinusoidally varying voltage (potential difference) or current
- The usual circuit-diagram symbol for an ac source is

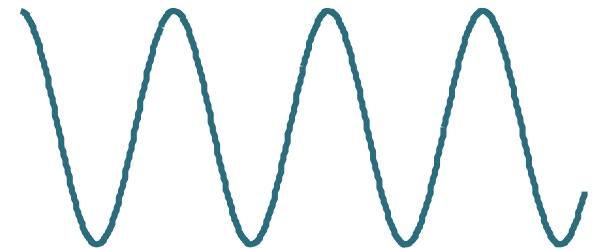


Sinusoids: Standard Form

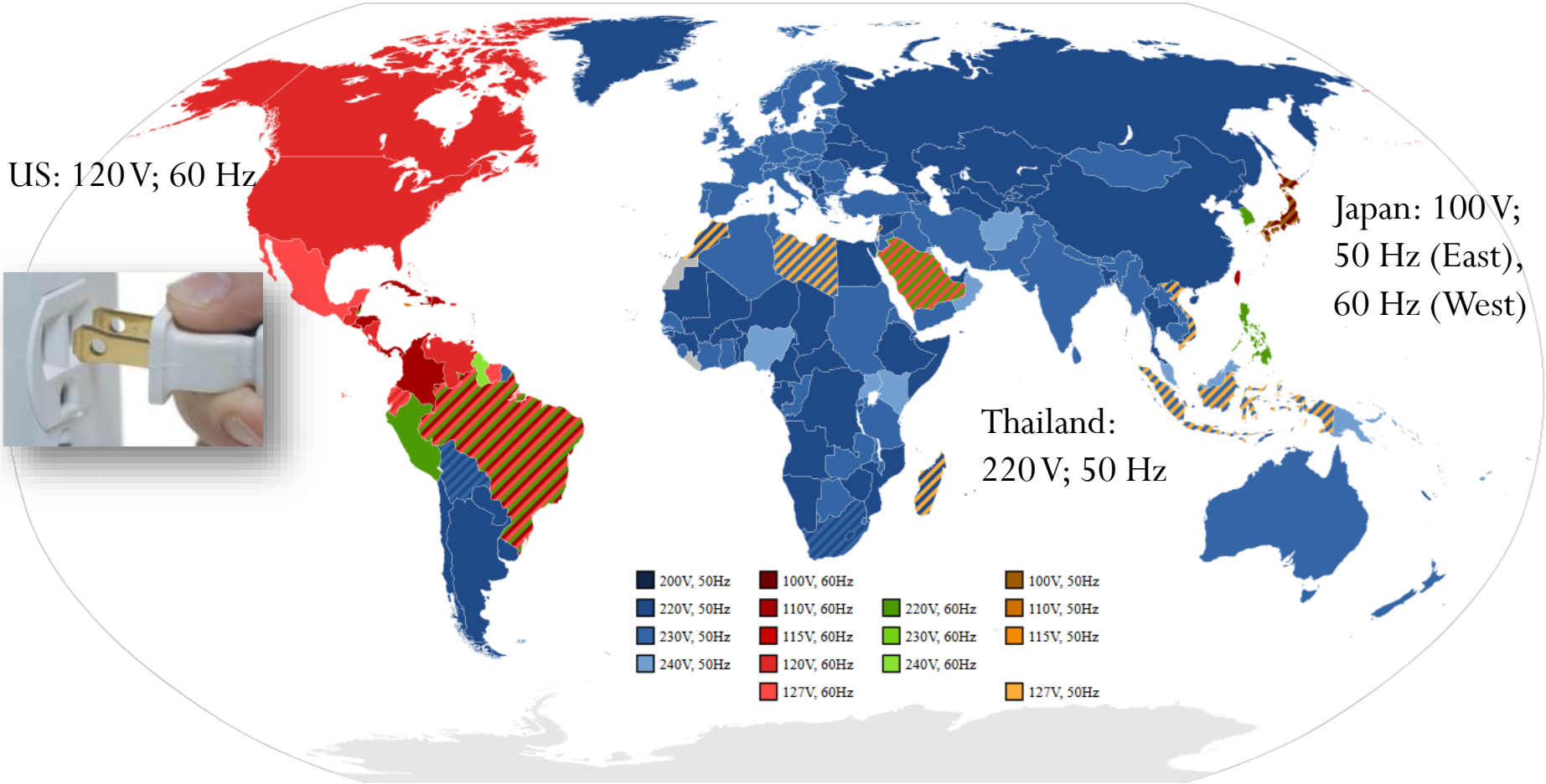
- General sinusoidal signal (in cosine form)

$$x(t) = X_m \cos(\omega t + \phi) = X_m \cos(2\pi f t + \phi).$$

- X_m : amplitude of the sinusoid
 - Nonnegative when expressed in standard form
- T : period (the time of one complete cycle)
- f : frequency
 - #cycles per second or hertz (Hz) $f = \frac{1}{T} = \frac{\omega}{2\pi}$
- ω : angular frequency in radians/s (or rad/s)
- ϕ : phase
 - Between -180° and $+180^\circ$ in standard form



Around the World: Voltages and Frequencies



Conversions to standard form

- When the signal is given in the sine form, it can be converted into its cosine form via the identity

$$\sin(x) = \cos(x - 90^\circ).$$

In particular,

$$X_m \sin(\omega t + \phi) = X_m \cos(\omega t + \phi - 90^\circ).$$

- We can avoid having X_m with negative sign by the following conversion:

$$-\cos(x) = \cos(x \pm 180^\circ).$$

In particular,

$$-A \cos(\omega t + \phi) = A \cos(2\pi ft + \phi \pm 180^\circ).$$

- Note that usually you do not have the choice between $+180^\circ$ or -180° . The one that you need to use is the one that makes $\phi \pm 180^\circ$ falls somewhere between -180° and $+180^\circ$.

Exercise

Express the following sinusoids in their standard forms

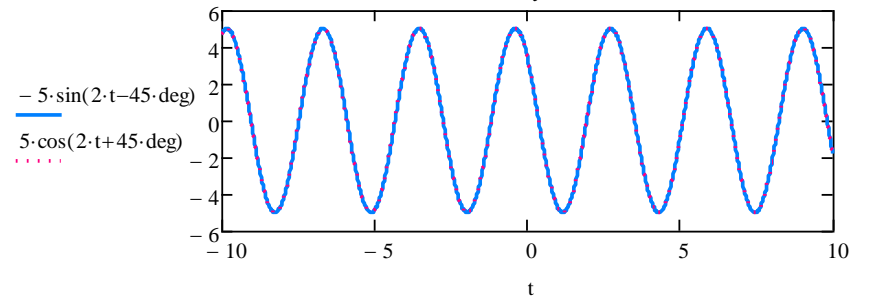
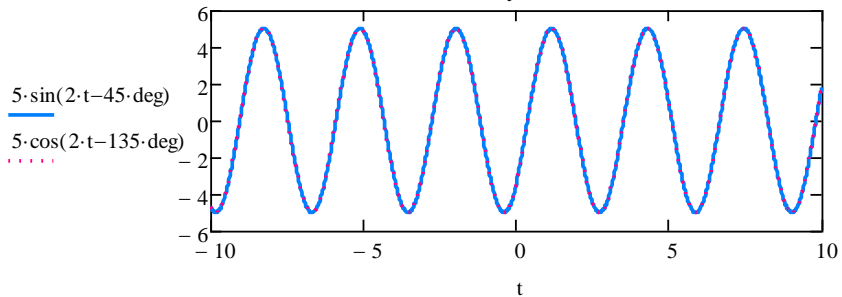
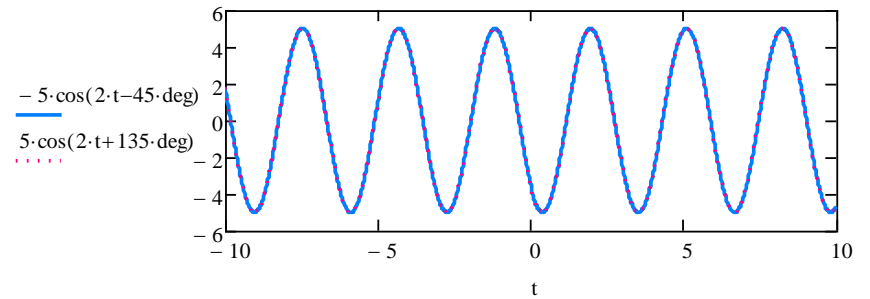
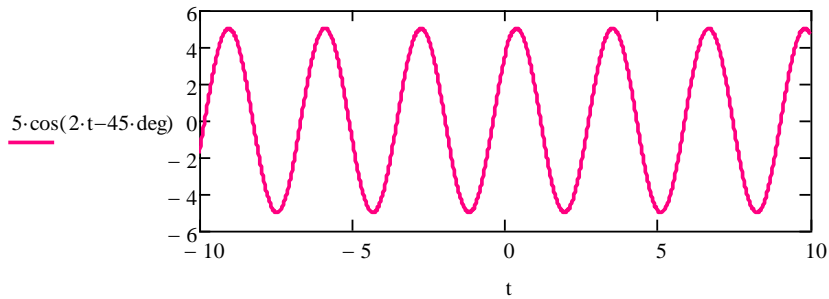
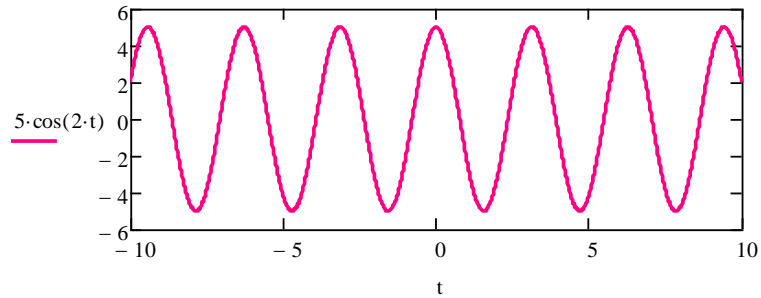
$$5 \cos(2t - 45^\circ) = 5 \cos(2t + (-45^\circ))$$

$$\begin{aligned} 5 \sin(2t - 45^\circ) &= 5 \cos(2t - 45^\circ - 90^\circ) \\ &= 5 \cos(2t + (-135^\circ)) \end{aligned}$$

$$\begin{aligned} -5 \cos(2t - 45^\circ) &= 5 \cos(2t - 45^\circ \pm 180^\circ) \\ &= 5 \cos(2t + 135^\circ) \end{aligned}$$

$$\begin{aligned} -5 \sin(2t - 45^\circ) &= +5 \cos(2t - \underbrace{45^\circ - 90^\circ}_{-135^\circ} \pm 180^\circ) \\ &= 5 \cos(2t + 45^\circ) \end{aligned}$$

Exercise



$$i = I_m \cos(\omega t + \phi_i)$$

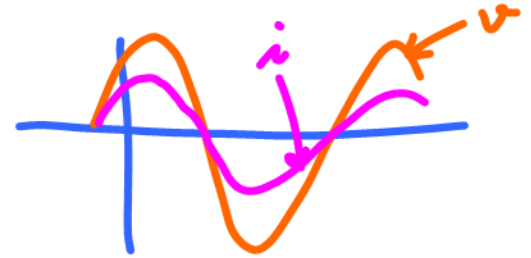


$$v = V_m \cos(\omega t + \phi_v)$$

$$v = R i$$

$$V_m \cos(\omega t + \phi_v) = R I_m \cos(\omega t + \phi_i)$$

$$\left\{ \begin{array}{l} V_m = R I_m \\ \phi_v = \phi_i \end{array} \right.$$



$$i = I_m \cos(\omega t + \phi_i)$$



$$v = V_m \cos(\omega t + \phi_v)$$

$$v = L \frac{di}{dt}$$

$$V_m \cos(\omega t + \phi_v) = \omega L I_m (-\sin(\omega t + \phi_i))$$

$$= \omega L I_m \cos(\omega t + \phi_i - 90^\circ \pm 180^\circ)$$

$$= \omega L I_m \cos(\omega t + \phi_i + 90^\circ)$$

$$V_m = (\omega L) I_m$$

$$\phi_v = \phi_i + 90^\circ$$

Application: Measuring Body Fat by Bioelectric Impedance Analysis

- The electrodes attached to this overweight patient's chest are applying a small ac voltage of frequency 50 kHz.
- The attached instrumentation measures the amplitude and phase angle of the resulting current through the patient's body.
- These depend on the relative amounts of water and fat along the path followed by the current, and so provide a sensitive measure of body composition.

